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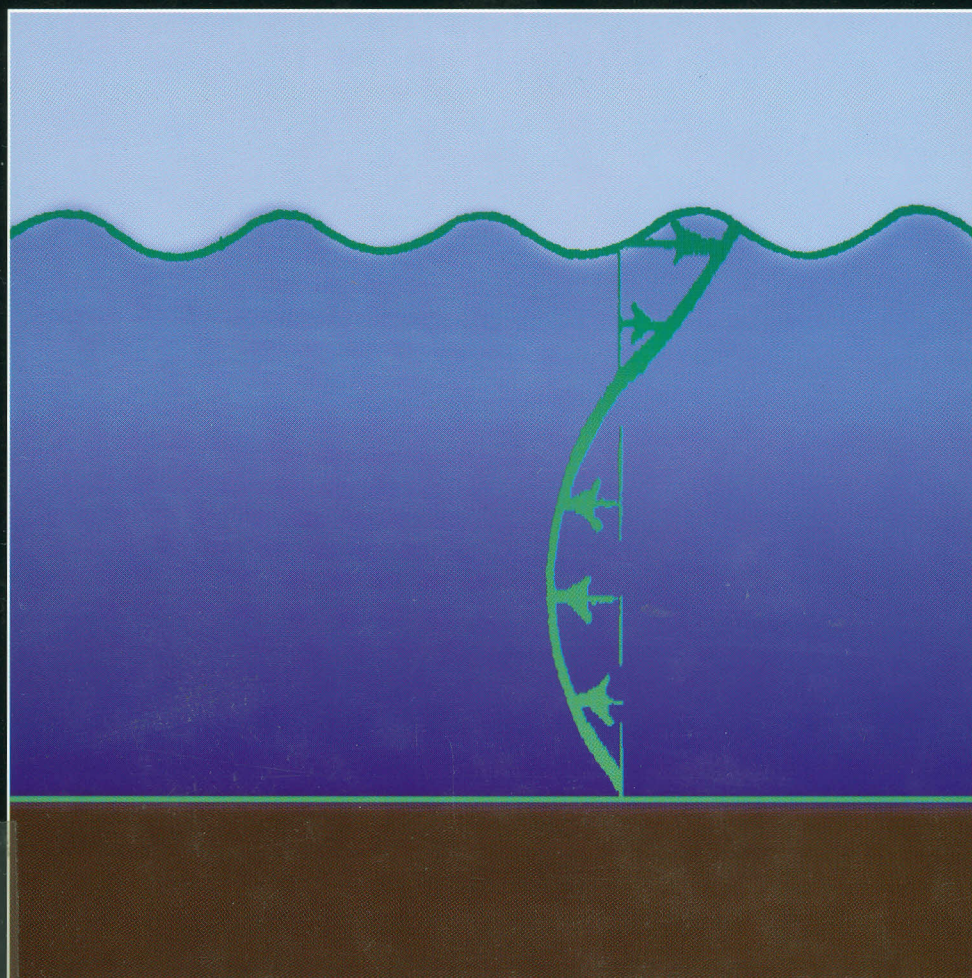


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PROPAGATION OF WAVES IN SHEAR FLOWS

A. L. Fabrikant & Yu. A. Stepanyants



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PROPAGATION OF WAVES IN SHEAR FLOWS

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CONTENTS

Preface	ix
Introduction	1
Chapter I. WAVE ENERGY AND MOMENTUM IN A MOVING MEDIUM	7
1.1. Wave momentum and quasi-particles	8
1.2. Momentum of a localized incompressible flow	14
1.3. Momentum of a wave-train induced flow. Long wave radiation	19
1.4. Absorption and scattering of a surface wave packet. Residual vortex	23
1.5. Ponderomotive force in an elastic medium. Induced flows for internal gravity waves	27
1.6. Acoustic wind	30
1.7. How to determine wave energy and momentum?	33
1.8. Negative energy waves in hydrodynamics	35
1.9. The relationship between kinetic and potential ener- gies of linear perturbations on a vortex sheet	40
1.10. Spectral evolution of a wave packet	46
1.10.1. The evolution of Schrödinger solitons	49
1.10.2. Mean flow dissipation. Fast envelope solitons ..	55
Chapter II. WAVE GENERATION BY UNSTABLE SHEAR FLOWS	59
2.1. Flow stability in an ideal fluid. Plasma-hydrodyna- mic analogy	59

2.2. The Miles' mechanism for wind wave generation	66
2.2.1. Waves on a flowing down sheet	71
Chapter III. PIECEWISE-LINEAR MODELS	
OF FLOWS	73
3.1. Negative energy waves and Kelvin-Helmholtz instability	74
3.2. Dissipative instability of a vortex sheet	78
3.3. Radiative instability	83
3.4. Nonlinear dynamics of long waves in hydrodynamic flows	89
3.4.1. The evolution of waves in media with long-wave instability	91
3.4.2. Waves in media with short-wave instability	96
3.5. Configuration instability of a vortex sheet in an incompressible fluid	99
3.6. Nonstationary vortex sheet	106
3.7. Waves on vorticity discontinuity	112
3.7.1. Algebraic Rayleigh's method. Interpretation of hydrodynamic instability	117
Chapter IV. OVER-REFLECTION	123
4.1. Miles-Ribner problem	123
4.2. Excitation of vortex sheet oscillations by an incident wave	128
4.3. Negative dissipation in a moving medium	131
4.4. Over-reflection of internal waves	134
4.5. Over-reflection of surface gravity waves	138
4.6. Rossby waves on a vortex sheet	141
Chapter V. RESONANT WAVE-FLOW INTERACTION	145
5.1. Resonant sound amplification	146
5.2. IGW amplification in a critical layer	152
5.2.1. The criterion of resonant amplification.	

Physical interpretation	158
5.2.2. Analytical and numerical investigations. Spontaneous radiation of IGW by critical layer	161
5.3. Internal waves in horizontally inhomogeneous shear flows	165
5.3.1. Vertical focusing of internal waves	171
5.4. Rossby waves in a critical layer	176

Chapter VI. OSCILLATORY SYSTEMS WITH HYDRODYNAMIC FLOWS 179

6.1. Aerodynamic generation of sound	179
6.2. Linear theory of whistle with a resonator	181
6.3. Acoustical analogs of electron micro-wave oscillators.	192
6.3.1. Travelling-wave tube	192
6.3.2. Monotron	195
6.3.3. Klystron	199
6.4. Radiative instability of streamlined oscillators in a moving fluid	201

Chapter VII. WAVES ON CONCENTRATED VORTICES 205

7.1. An algebraic method for columnar vortices	206
7.2. Wave amplification by a vortex with a viscous core: Zel'dovich's effect in hydrodynamics	220
7.3. Resonant wave amplification by vortices in a perfect fluid	222
7.4. Scattering of long waves	226

Chapter VIII. REMOTE WAVE SENSING OF MOVING VORTICES 229

8.1. Acoustic and internal wave scattering at vortices in a stratified rotating medium	230
8.2. Wave scattering at a system of point vortices	236
8.3. Remote acoustic sensing of moving vortices	239
8.3.1. Periodic vortex wake	240
8.3.2. Vortex rings	247

8.4. Internal gravity wave scattering at dipole vortices 252

Bibliography **261**

Chapter VI OSCILLATORY SYSTEMS WITH HYDRODYNAMIC FLOWS 179

6.1. A linear theory of vortices with a resonant internal gravity wave 179

Chapter VII WAVES ON CONCENTRATED VORTICES

7.1. An eigenvalue problem for vortices with a resonant internal gravity wave 205

Chapter VIII RESONANT WAVE SCATTERING OF MOVING VORTICES

8.1. Resonant wave scattering at a moving vortex 230